

RD Sharma
Solutions Class
12 Maths
Chapter 13
Ex 13.1

Derivatives as a Rate Measurer Ex 13.2 Q1

Let total surface area of the cylinder be A

$$A = 2\pi r(h + r)$$

Differentiating it with respect to r as r varies

$$\begin{aligned}\frac{dA}{dr} &= 2\pi r(0 + 1) + (h + r)2\pi \\ &= 2\pi r + 2\pi h + 2\pi r\end{aligned}$$

$$\frac{dA}{dr} = 4\pi r + 2\pi h$$

Derivatives as a Rate Measurer Ex 13.1 Q2

Let D be the diameter and r be the radius of sphere,

So, volume of sphere = $\frac{4}{3}\pi r^3$

$$v = \frac{4}{3}\pi \left(\frac{D}{2}\right)^3$$

$$v = \frac{4}{24}\pi D^3$$

Differentiating it with respect to D .

$$\frac{dv}{dD} = \frac{12}{24}\pi D^2$$

$$\frac{dv}{dD} = \frac{\pi D^2}{2}$$

Derivatives as a Rate Measurer Ex 13.1 Q3

Given, radius of sphere (r) = 2cm.

We know that,

$$v = \frac{4}{3}\pi r^3$$

$$\frac{dv}{dr} = 4\pi r^2 \quad \text{--- (i)}$$

And $A = 4\pi r^2$

$$\frac{dA}{dr} = 8\pi r \quad \text{--- (ii)}$$

Dividing equation (i) by (ii),

$$\frac{\frac{dv}{dr}}{\frac{dA}{dr}} = \frac{4\pi r^2}{8\pi r}$$

$$\frac{dv}{dA} = \frac{r}{2}$$

$$\left(\frac{dv}{dA}\right)_{r=2} = 1$$

Derivatives as a Rate Measurer Ex 13.1 Q4

Let r be two radius of circular disc.

We know that,

$$\text{Area } A = \pi r^2$$

$$\frac{dA}{dr} = 2\pi r \quad \text{--- (i)}$$

Circumference $C = 2\pi r$

$$\frac{dC}{dr} = 2\pi \quad \text{--- (ii)}$$

Dividing equation (i) by (ii),

$$\frac{\frac{dA}{dr}}{\frac{dC}{dr}} = \frac{2\pi r}{2\pi}$$

$$\frac{dA}{dC} = r$$

$$\left(\frac{dA}{dC}\right)_{r=3} = 3$$

Derivatives as a Rate Measurer Ex 13.1 Q5

Let r be the radius, v be the volume of cone and h be height

$$v = \frac{1}{3} \pi r^2 h$$

$$\frac{dv}{dr} = \frac{2}{3} \pi r h.$$

Derivatives as a Rate Measurer Ex 13.1 Q6

Let r be radius and A be area of circle, so

$$A = \pi r^2$$

$$\frac{dA}{dr} = 2\pi r$$

$$\left(\frac{dA}{dr}\right)_{r=5} = 2\pi (5)$$

$$\left(\frac{dA}{dr}\right)_{r=5} = 10\pi$$

Derivatives as a Rate Measurer Ex 13.1 Q7

Here, $r = 2$ cm

$$v = \frac{4}{3} \pi r^3$$

$$\frac{dv}{dr} = 4\pi r^2$$

$$\left(\frac{dv}{dr}\right)_{r=2} = 4\pi (2)^2$$

$$\left(\frac{dv}{dr}\right)_{r=2} = 16\pi$$

Derivatives as a Rate Measurer Ex 13.1 Q8

Marginal cost is the rate of change of total cost with respect to output.

$$\therefore \text{Marginal cost (MC)} = \frac{dC}{dx} = 0.007(3x^2) - 0.003(2x) + 15$$

$$= 0.021x^2 - 0.006x + 15$$

$$\text{When } x = 17, \text{ MC} = 0.021(17^2) - 0.006(17) + 15$$

$$= 0.021(289) - 0.006(17) + 15$$

$$= 6.069 - 0.102 + 15$$

$$= 20.967$$

Hence, when 17 units are produced, the marginal cost is Rs. 20.967

Derivatives as a Rate Measurer Ex 13.1 Q9

Marginal revenue is the rate of change of total revenue with respect to the number of units sold.

$$\therefore \text{Marginal Revenue (MR)} = \frac{dR}{dx} = 13(2x) + 26 = 26x + 26$$

When $x = 7$,

$$\text{MR} = 26(7) + 26 = 182 + 26 = 208$$

Hence, the required marginal revenue is Rs 208.

Derivatives as a Rate Measurer Ex 13.1 Q10

$$R(x) = 3x^2 + 36x + 5$$

$$\frac{dR}{dx} = 6x + 36$$

$$\left. \frac{dR}{dx} \right|_{x=5} = 6 \times 5 + 36$$

$$= 30 + 36$$

$$= 66$$

This, as per the question, indicates the money to be spent on the welfare of the employees, when the number of employees is 5.